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**Normality of topological groups revisited**

by

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**Abstract**

It was proved by Stone in the 60's that  $\mathbb{N}^{\mathbb{R}}$ , the uncountable product of copies of  $\mathbb{N}$ , is not a normal topological space. The same proof can be used to conclude that the uncountable product of copies of the group of integers,  $G := \mathbb{Z}^{\mathbb{R}}$  is a nonnormal abelian topological group. We have further proved that, any locally quasi-convex group topology  $\nu$  on  $G$  which gives rise to the same character group as  $G$  with its original topology, say  $G^\wedge$ , is nonnormal.

In this talk we shall face the following question: Under which conditions on a fixed group duality  $(G, G^\wedge)$  are there locally quasi-convex compatible normal topologies?

(The talk is based upon joint work with V. Pérez Valdés)